

# DISTRIBUTED COGNITIVE MAC FOR ENERGY-CONSTRAINED OPPORTUNISTIC SPECTRUM ACCESS

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## ABSTRACT

We address the design of distributed cognitive medium access control (MAC) protocols for opportunistic spectrum access (OSA) under an energy constraint on the secondary users. The objective is to maximize the expected number of information bits that can be delivered by a secondary user during its battery lifetime without causing interference to primary users. By absorbing the residual energy level of the secondary user into the state space, we formulate the energy-constrained OSA problem as an unconstrained partially observable Markov decision process (POMDP) and obtain the optimal spectrum sensing and access policy. We analyze and reduce the computational complexity of the optimal policy. We also propose a suboptimal solution to energy-constrained OSA, whose computational complexity can be systematically traded off with its performance. Numerical examples are provided to study the impact of spectrum occupancy dynamics, channel fading statistics, and energy consumption characteristics of the secondary user on the optimal sensing and access decisions.

## I. INTRODUCTION

The exponential growth in wireless services has resulted in an overly crowded spectrum. In contrast to the apparent spectrum scarcity is the pervasive existence of spectrum opportunities. Real measurements show that, at any given time and location, a large portion of licensed spectrum lies unused [1]. Even when a frequency band is actively used, the bursty arrivals of many applications result in abundant spectrum opportunities at the millisecond scale. This has motivated opportunistic spectrum access (OSA), envisioned by the DARPA XG program [2]. The idea of OSA is to allow secondary users to identify and exploit spectrum opportunities under the constraint that they do not cause harmful interference to primary users.

There is a growing body of literature on the design of medium access control (MAC) for OSA [3]–[8]. Most existing works (see [3]–[6]) consider a network of geographically distributed secondary users, each affected by a different set of primary users whose spectrum access activities are static or slowly varying

in time. The design objective is to allocate these spatially varying spectrum opportunities among secondary users so that the network-level spectrum efficiency is maximized subject to some regulatory constraint on interference to primary users.

The exploitation of temporal spectrum opportunities resulting from the bursty traffic of primary users has been studied in [7], [8]. Within the framework of partially observable Markov decision process (POMDP), the optimal cognitive MAC protocol that allows secondary users to independently search for and exploit instantaneous spectrum opportunities has been developed in [7]. This MAC protocol consists of a sensing strategy that determines which channels in the spectrum to sense based on spectrum occupancy dynamics and an access strategy that determines whether to transmit over the sensed channels based on sensing outcomes. The energy constraint of secondary users is, however, not taken into account in [7], [8].

The incorporation of energy constraint can significantly complicate the cognitive MAC design. Under the energy constraint, sensing decisions should be made based on not only the spectrum occupancy dynamics but also channel fading statistics, and access decisions should take into account not only the availability but also the fading condition of the sensed channel. This makes the optimal sensing and access strategies opportunistic in both spectrum and time. Even the residual energy level of the secondary user will play an important role in decision-making. For example, when the battery is depleting, should the user wait for increasingly better channel realizations for transmission or should it lower the requirement on channel given that sensing also costs energy? Clearly, such decisions depend on the energy consumption characteristics of secondary users.

As a starting point to energy-constrained OSA, this paper aims to develop the fundamental limit on the expected number of information bits that can be delivered by a secondary user during its battery lifetime. By absorbing the residual energy level of the secondary user into the state space, we show that the energy-constrained OSA problem can be formulated as an unconstrained POMDP. Based on the theory of POMDP, we obtain the optimal sensing and access policy which not only provides a performance benchmark but also enables us to study the impact of spectrum occupancy dynamics, channel fading statistics, and energy consumption characteristics of the secondary user on the optimal sensing and access decisions. However, our complexity analysis indicates that the optimal policy is computationally expensive. We therefore exploit the underlying structure of the problem

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to reduce the computational complexity of the optimal policy. We also provide a suboptimal solution whose computational complexity can be systematically traded off with its performance. Referred to as the greedy- $w$  strategy, this approach maximizes the throughput of the secondary user in a fixed time window of  $w$  slots. Simulation result shows that as the window size  $w$  increases, the performance of the greedy- $w$  strategy quickly approaches the optimal performance.

## II. PROBLEM STATEMENT

Consider a spectrum consisting of  $N$  slotted channels, each with bandwidth  $B_n$  ( $n = 1, \dots, N$ ). The spectrum is licensed to a primary network. Let  $S_n \in \{0\text{ (occupied)}, 1\text{ (idle)}\}$  denote the availability of channel  $n$  in a slot. We assume that the spectrum occupancy  $\mathbf{S} \triangleq [S_1, \dots, S_N] \in \{0, 1\}^N$  follows a discrete Markov process with  $2^N$  states.

We consider an ad hoc secondary network where there is no central coordinator or dedicated communication/control channel. Secondary users, each powered by a battery with initial energy  $\mathcal{E}_0$ , independently seek instantaneous spectrum opportunities in these  $N$  channels. At the beginning of each slot, a secondary user with data to transmit chooses at most  $M$  ( $1 \leq M \leq N$ ) channels to sense and then decides whether to access these channels according to the sensing outcomes. Our goal is to determine the sensing and access decisions sequentially in each slot so as to maximize the total expected number of information bits that can be delivered by a secondary user during its battery lifetime. For ease of presentation, we assume  $M = 1$ . Our results can be generalized to  $M > 1$ .

### A. Protocol Structure

A channel only presents an opportunity to a pair of secondary users if it is available at both the transmitter and the receiver. Hence, spectrum opportunities need to be identified jointly by the transmitter and the receiver [9]. Next, we briefly comment on the implementation of the protocol.

Suppose that the transmitter and the receiver have tuned to the same channel after the initial handshake as described in [9]. At the beginning of a slot, the transmitter and the receiver hop to same channel<sup>1</sup>. If the channel is sensed to be available, the transmitter generates a random backoff time. If the channel remains idle when its backoff time expires, it transmits a short request-to-send (RTS) message to the receiver, indicating that the channel is available at the transmitter. Upon receiving the RTS, the receiver estimates the channel fading condition using the RTS, and then replies with a clear-to-send (CTS) message if the channel is also available at the receiver. The receiver also informs the transmitter of the current fading condition by piggybacking the estimated channel state to the CTS. After a successful exchange of RTS-CTS, the transmitter and the receiver can communicate over this channel. At the end of this slot, the receiver acknowledges every successful data transmission. Note that at the beginning of each slot, the transmitter and the receiver

<sup>1</sup>Note that the protocols developed in this paper can ensure the transceiver synchronization without the help of any dedicated communication or control channel. See details in III-C.

can also choose not to hop to any channel and turn to sleep mode until the beginning of next slot.

### B. Energy Model

We assume that channels between the secondary user and its destination follow a block fading model. That is, the channel gain in a slot is a random variable (RV) identically and independently distributed (i.i.d.) across slots but not necessarily i.i.d. across channels.

Let  $E_s(n)$  and  $E_{tx}(n)$  denote, respectively, the energy consumed in sensing and accessing channel  $n$  in a slot. For simplicity, we assume that sensing energy consumption  $E_s(n)$  is identical for all channels:  $E_s(n) = e_s$  for every  $n$ . Note that the transmission energy consumption  $E_{tx}(n)$  is a RV depending on the current fading condition of channel  $n$ . In general, the better the channel condition, the lower the required transmission energy. Let  $L$  be the number of power levels at which the secondary user can transmit and  $\varepsilon_k$  the energy consumed in transmitting at the  $k$ -th power level in a slot. The transmission energy consumption  $E_{tx}(n)$  thus has realizations restricted to a finite set  $\mathcal{E}_{tx}$  given by

$$E_{tx}(n) \in \mathcal{E}_{tx} \triangleq \{\varepsilon_k\}_{k=0}^L, \quad (1)$$

where  $0 < \varepsilon_1 < \dots < \varepsilon_L < \infty$  and  $\varepsilon_0 = 0$  indicates that the secondary user does not transmit. We also consider the energy  $e_p$  consumed in sleeping mode of the secondary user.

Let  $E$  denote the residual energy level of a secondary user at the beginning of a slot. Note that  $E$  is a RV determined by the channel conditions and the sensing and access decisions in all previous slots. Thus,  $E$  belongs to finite set  $\mathcal{E}_r$  given by

$$E \in \mathcal{E}_r \triangleq \{e : e = \mathcal{E}_0 - \sum_{k=0}^L c_k(e_s + \varepsilon_k) - ce_p, \\ e \geq 0, c, c_k \geq 0, c, c_k \in \mathbb{Z}\} \cup \{0\}, \quad (2)$$

where  $c_k$  is the number of slots when the secondary user chooses to sense a channel and then transmit over it at the  $k$ -th power level and  $c$  is the number of slots when the secondary user turns to sleeping mode.

## III. OPTIMAL ENERGY-CONSTRAINED OSA

The energy-constrained OSA can be formulated a constrained POMDP, which is usually more difficult to solve than an unconstrained one. By absorbing the residual energy level of the secondary user into the state space, we reduce a constrained POMDP to an unconstrained one. Based on the theory of POMDP, we obtain the spectrum optimal sensing and access policy.

### A. An Unconstrained POMDP Formulation

*State Space* In each slot, the network state is characterized by the current spectrum occupancy  $\mathbf{S} \in \{0, 1\}^N$  and the residual energy level  $E \in \mathcal{E}_r$  of the secondary user at the beginning of this slot. The state space  $\mathcal{S}$  can be defined as

$$(\mathbf{S}, E) \in \mathcal{S} \triangleq \{(\mathbf{s}, e) : \mathbf{s} \in \{0, 1\}^N, e \in \mathcal{E}_r\}. \quad (3)$$

*Action Space* After the state transition of spectrum occupancy at the beginning of each slot, the secondary user can either choose a channel  $a \in \{1, \dots, N\}$  to sense or turn to sleep ( $a = 0$ ). If the secondary user chooses channel  $a$  to sense, then it will obtain a sensing outcome  $\Theta_a \in \{0, 1, \dots, L\}$  which reflects the occupancy state and the fading condition of the chosen channel:  $\Theta_a = 0$  indicates that channel  $a$  is busy (*i.e.*,  $S_a = 0$ ) and  $\Theta_a = k$  ( $k = 1, \dots, L$ ) indicates that channel  $a$  is idle (*i.e.*,  $S_a = 1$ ) and the fading condition requires the secondary user to transmit at the  $k$ -th power level (*i.e.*,  $E_{\text{tx}}(a) = \varepsilon_k$ ). Given sensing outcome  $\Theta_a$ , the secondary user decides whether to transmit over the chosen channel. Let  $\Phi_a(k) \in \{0 \text{ no access}, 1 \text{ access}\}$  ( $k = 0, \dots, L$ ) denote the access decision under sensing outcome  $\Theta_a = k$ . Since we have assumed perfect spectrum sensing, the access decision under  $\Theta_a = 0$  (busy) is simple:  $\Phi_a(0) = 0$  (no access). In this case, secondary users will not collide with primary users.

The action space  $\mathcal{A}$  consists of all sensing decisions  $a$  and access decisions  $\Phi_a \triangleq [\Phi_a(1), \dots, \Phi_a(L)]$ :

$$(a, \Phi_a) \in \mathcal{A} \triangleq \{(0, [0, \dots, 0])\} \cup \{(a, \phi) : a \in \{1, \dots, N\}, \phi \triangleq [\phi(1), \dots, \phi(L)] \in \{0, 1\}^L\}. \quad (4)$$

Note that the access decision  $\Phi_0$  associated with sensing action  $a = 0$  (sleeping mode) is determined by  $\Phi_0(k) = 0$  for all  $1 \leq k \leq L$ .

*Network State Transition* Recall that the network state consists of two parts: the spectrum occupancy  $\mathbf{S}$  and the residual energy  $E$  of the secondary user. At the beginning of each slot, the spectrum occupancy  $\mathbf{S}$  transits independently of the residual energy  $E$  according to transition probabilities  $\{p_{\mathbf{s}, \mathbf{s}'}\}$ , where  $p_{\mathbf{s}, \mathbf{s}'}$  denotes the probability that the spectrum occupancy state transits from  $\mathbf{s} \in \{0, 1\}^N$  to  $\mathbf{s}' \in \{0, 1\}^N$ . In this paper, we assume that the spectrum occupancy dynamics  $\{p_{\mathbf{s}, \mathbf{s}'}\}$  are known and remain unchanged during the battery lifetime of the secondary user.

If the secondary user decides to choose channel  $a \in \{1, \dots, N\}$  to sense in this slot, then it will consume  $e_s$  in sensing and  $\Phi_a(\Theta_a)\varepsilon_{\Theta_a}$  in transmitting. Thus, at the end of this slot, the residual energy of the secondary user reduces to  $E' = \mathcal{T}_E(E \mid a, \Theta_a, \Phi_a(\Theta_a))$ :

$$\begin{aligned} & \mathcal{T}_E(E \mid a, \Theta_a, \Phi_a(\Theta_a)) \\ &= \begin{cases} E - e_p, & a = 0, \\ \max\{E - e_s - \Phi_a(\Theta_a)\varepsilon_{\Theta_a}, 0\}, & a \neq 0, \end{cases} \end{aligned} \quad (5)$$

where  $e_p$  is energy consumed in the sleeping mode.

*Observations* Due to partial spectrum sensing, the secondary user does not have full knowledge of the spectrum occupancy state in each slot. It, however, can obtain the occupancy state of the chosen channel  $a \in \{1, \dots, N\}$  from sensing outcome (*i.e.*, observation)  $\Theta_a \in \{0, 1, \dots, L\}$ . Let  $q_s^{(a)}(k)$  be the probability that the secondary user observes  $\Theta_a = k$  in the chosen channel  $a$  given current spectrum occupancy state  $\mathbf{S} = \mathbf{s}$ . Under perfect spectrum sensing, we have that

$$\begin{aligned} q_s^{(a)}(k) &= \Pr\{\Theta_a = k \mid \mathbf{S} = \mathbf{s}\} \\ &= \begin{cases} 1_{[k \neq 0]} p_a(k), & \text{if } a \neq 0, s_a = 1, \\ 1_{[k=0]}, & \text{if } a \neq 0, s_a = 0, \end{cases} \end{aligned} \quad (6)$$

where  $p_a(k) \triangleq \Pr\{E_{\text{tx}}(a) = \varepsilon_k\}$  is the probability that the fading condition of channel  $a$  requires the secondary user to transmit at the  $k$ -th power level, and  $1_{[x]}$  is the indicator function:  $1_{[x]} = 1$  if  $x$  is true and 0 otherwise. Note that  $\{p_a(k)\}_{k=1}^L$  are determined by the fading statistics of channel  $a$  and are independent of the spectrum occupancy state. From (6), we can see that  $\sum_{k=0}^L q_s^{(a)}(k) = 1$  for any spectrum occupancy state  $\mathbf{s} \in \mathcal{S}$  and any chosen channel  $a \in \{1, \dots, N\}$ .

Note that if the secondary user turns to sleep, then it will not have any sensing outcome. We can define  $\{q_s^{(0)}(k)\}$  as arbitrary values that satisfy  $\sum_{k=0}^L q_s^{(0)}(k) = 1$ . For simplicity, we define  $q_s^{(0)}(k) = 1_{[k=0]}$ .

*Reward Structure* At the end of each slot, the secondary user obtains a non-negative reward  $R_{E, \Theta_a}^{(a, \Phi_a(\Theta_a))}$  depending on its residual energy  $E$  at the beginning of this slot, the sensing outcome  $\Theta_a$ , and the sensing and access decisions  $(a, \Phi_a(\Theta_a))$ . Assuming that the number of information bits that can be transmitted over a channel in one slot is proportional to the channel bandwidth, we define immediate reward  $R_{E, \Theta_a}^{(a, \Phi_a(\Theta_a))}$  as

$$R_{E, \Theta_a}^{(a, \Phi_a(\Theta_a))} \triangleq \begin{cases} 0, & a = 0, \\ \Phi_a(\Theta_a)B_a 1_{[E - e_s - \varepsilon_{\Theta_a} \geq 0]}, & a \neq 0. \end{cases} \quad (7)$$

That is, a reward is obtained if and only if the secondary chooses to sense and access (*i.e.*,  $a \neq 0$ ,  $\Phi_a(\Theta_a) = 1$ ) an idle channel (*i.e.*,  $\Theta_a \neq 0$ ) and its residual energy is enough to cope with the channel fade in the selected channel (*i.e.*,  $E - e_s - \varepsilon_{\Theta_a} \geq 0$ ). Note that no reward will be accumulated once the battery energy level drops below  $e_s + \varepsilon_1$ , where  $\varepsilon_1$  is the least required transmission energy. Hence, the total expected accumulated reward represents the total expected number of information bits that can be delivered by the secondary user during its battery lifetime.

*Belief State* At the beginning of a slot, the secondary user has the information of its own residual energy  $E$  but not the current spectrum occupancy state  $\mathbf{S}$ . Its knowledge of  $\mathbf{S}$  based on all past decisions and observations can be summarized by a belief state  $\boldsymbol{\lambda} = \{\lambda_s\}_{s \in \{0, 1\}^N}$  [10], where  $\lambda_s$  is the conditional probability (given the decision and observation history) that the network state is  $\mathbf{S} = \mathbf{s}$  at the beginning of this slot prior to the transition in the spectrum occupancy state.

At the end of a slot, the secondary user can update the belief state  $\boldsymbol{\lambda}$  for future use based on sensing action  $a$  and sensing outcome  $\Theta_a$  in this slot. Specifically, let  $\boldsymbol{\lambda}' \triangleq \mathcal{T}_{\boldsymbol{\lambda}}(\boldsymbol{\lambda} \mid a, k)$  denote the updated belief state whose element  $\lambda'_s$  denotes the probability that the current spectrum occupancy state is  $\mathbf{S} = \mathbf{s}$  given belief state  $\boldsymbol{\lambda}$  at the beginning of this slot and the observation  $\Theta_a = k$  of chosen channel  $a$  in the current slot. Applying Bayes rule, we obtain  $\lambda'_s$  as

$$\begin{aligned} \lambda'_s &= \Pr\{\mathbf{S} = \mathbf{s} \mid \boldsymbol{\lambda}, a, k\} \\ &= \begin{cases} \frac{\sum_{s'} \lambda_{s'} p_{s', s}}{\sum_{s'} \lambda_{s'} p_{s', s} 1_{[s_a = 1_{[k \neq 0]}]}}, & a = 0, \\ \frac{\sum_{s''} \sum_{s'} \lambda_{s'} p_{s', s''} 1_{[s_a' = 1_{[k \neq 0]}]}}{\sum_{s''} \sum_{s'} \lambda_{s'} p_{s', s''} 1_{[s_a' = 1_{[k \neq 0]}]}}, & a \neq 0, \end{cases} \end{aligned} \quad (8)$$

where the summations are taken over the space  $\{0, 1\}^N$  of spectrum occupancy state  $\mathbf{S}$ . Note that when the secondary user

turns to sleeping mode ( $a = 0$ ), no observation is made and the belief state is updated according to the spectrum occupancy dynamics  $\{p_{\mathbf{s}, \mathbf{s}'}\}$ .

*Unconstrained POMDP Formulation* We have formulated the energy-constrained OSA as a POMDP problem. A policy  $\pi$  of this POMDP is defined as a sequence of functions:

$$\pi \triangleq [\mu_1, \mu_2, \dots], \quad \mu_t : [0, 1]^{2^N} \times \mathcal{E}_r \rightarrow \mathcal{A},$$

where  $\{a, \Phi_a\} = \mu_t(\lambda, E)$  maps every information state  $(\lambda, E)$ , which consists of belief state  $\lambda \in [0, 1]^{2^N}$  and residual energy  $E \in \mathcal{E}_r$ , at the beginning of slot  $t$  to a sensing decision  $a \in \{0, 1, \dots, N\}$  and a set of access decisions  $\Phi_a = [\Phi_a(1), \dots, \Phi_a(L)] \in \{0, 1\}^L$ .

The design objective is to find the optimal policy  $\pi^*$  that maximizes the total expected reward:

$$\pi^* = \arg \max_{\pi} \mathbb{E}_{\pi} \left[ \sum_{t=1}^{\infty} R_{(\mathbf{S}, E), \Theta_a}^{(a, \Phi_a(\Theta_a))}(t) \mid \lambda_0 \right], \quad (9)$$

where  $\lambda_0$  is the initial belief state given by the stationary distribution of spectrum occupancy. We thus have an unconstrained POMDP.

### B. Optimal Policy

Let  $V(\lambda, E)$  be the value function, which denotes the maximum expected remaining reward that can be accrued when the current information state is  $(\lambda, E)$ . We notice from (7) that the value function is given by  $V(\lambda, E) = 0$  for any information state  $(\lambda, E)$  with residual energy  $E < e_s + \varepsilon_1$ . For any other information state, its value function  $V(\lambda, E)$  is the unique solution to the following equation:

$$V(\lambda, E) = \max_{(a, \phi) \in \mathcal{A}} \sum_{k=0}^L u_k^{(a)} [R_{E, k}^{(a, \phi(k))} + V(\mathcal{T}_{\lambda}(\lambda | a, k), \mathcal{T}_E(E | a, k, \phi(k)))], \quad (10)$$

where  $\mathcal{T}_{\lambda}(\lambda | a, k)$  is the updated belief state given in (8),  $\mathcal{T}_E(E | a, k, \phi(k))$  is the reduced battery energy given in (5), and  $u_k^{(a)} \triangleq \Pr\{\Theta_a = k | \lambda\}$  is the probability of observing  $\Theta_a = k$  given belief state  $\lambda$ , which is determined by the spectrum occupancy dynamics and the channel fading statistics:

$$u_k^{(a)} = \sum_{\mathbf{s}' \in \{0, 1\}^N} \lambda_{\mathbf{s}'} \sum_{\mathbf{s} \in \{0, 1\}^N} p_{\mathbf{s}', \mathbf{s}} q_{\mathbf{s}}^{(a)}(k). \quad (11)$$

In principle, by solving (10), we can obtain the optimal sensing and access actions  $(a^*, \Phi_a^*)$  that achieve the maximum expected reward  $V(\lambda, E)$  for each possible information state  $(\lambda, E)$ . We can also obtain the maximum expected number of information bits  $V_{opt}$  that can be delivered by a secondary user during its battery lifetime as  $V_{opt} = V(\lambda_0, \mathcal{E}_0)$ , where  $\lambda_0$  is the initial belief state.

### C. Transceiver Synchronization

Without a dedicated communication or control channel, transceiver synchronization is a key issue in distributed MAC design for OSA networks [9]. Specifically, a secondary user and its intended receiver need to hop to the same channel at the

beginning of each slot in order to carry out the communication [9]. Here we show that the optimal sensing and access policy developed in Section III-B ensures transceiver synchronization.

The protocol structure described in Section II-A ensures that both the transmitter and the receiver have the same information on the occupancy state and the fading condition of the sensed channel in each slot. Hence, at the end of each slot, the transmitter and the receiver will reach the same updated belief state  $\lambda$  using (8) and the same residual energy  $E$  of the transmitter using (5). Since the channel selection is determined by the information state  $(\lambda, E)$ , the transmitter and the receiver will hop to the same channel in the next slot, *i.e.*, transceiver synchronization is maintained.

## IV. OPTIMAL POLICY WITH REDUCED COMPLEXITY

Although the value function given in (10) can be solved iteratively, it is computationally expensive. In this section, we first identify the sources of high complexity of the optimal policy and then reduce the complexity accordingly.

### A. Complexity of the Optimal Policy

We measure the computational complexity of a policy as the number of multiplications required to obtain all sensing and access actions during the secondary user's battery lifetime  $T$  when initial belief state and battery energy are given.

From (10), we notice that the optimal sensing and access action in the first slot depends on the value functions of all possible information states during the battery lifetime  $T$ . Hence, the computational complexity of the optimal policy is determined by the number of multiplications required to calculate the value functions of all possible information states.

Following the complexity analysis in [11], we can calculate the number of all possible information states  $(\lambda, E)$  during the secondary user's battery lifetime. Specifically, noting from (8) that the updated belief state is the same under all non-zero sensing outcomes ( $k \neq 0$ ), we can see that each information state  $(\lambda, E)$  can transit to at most  $L + 1$  different information states under sensing action  $a \neq 0$  but only one under sensing action  $a = 0$ . Hence, for fixed initial information state  $(\lambda_0, \mathcal{E}_0)$ , the number of all possible information states is on the order of  $\mathcal{O}((N(L+1))^{T-1})$ , which is exponential in the battery lifetime  $T$  and polynomial in the number  $N$  of channels. Moreover, from (10) and (11), we can see that it requires  $\mathcal{O}(3|\mathcal{A}|2^N 2^N (L+1))$  multiplications to calculate each value function, where  $|\mathcal{A}|$  is the size of the action space,  $2^N$  is the dimension of the belief state, and  $L+1$  is the number of possible observations. Therefore, the computational complexity of the optimal policy is on the order of  $\mathcal{O}(3|\mathcal{A}|2^N 2^N (L+1)(N(L+1))^{T-1})$ . We can see that the complexity is mainly caused by the following three factors: 1) the number  $\mathcal{O}((N(L+1))^{T-1})$  of possible information states; 2) the size  $|\mathcal{A}|$  of the action space, and 3) the dimension  $2^N$  of the belief state. We will address the first factor in Section V. In this section, we focus on the other two factors.

## B. Reduction of Action Space Size

Careful inspection of (5), (7) and (10) reveals that the quantity  $R_{E,k}^{(a,\phi(k))} + V(\mathcal{T}_\lambda(\boldsymbol{\lambda} | a, k), \mathcal{T}_E(E | a, k, \phi(k)))$  inside the square parenthesis of (10) only depends on the  $k$ -th entry  $\phi(k)$  of the access decision  $\phi$  and is independent of  $\phi(i)$  ( $i \neq k$ ). We can thus simplify (10) as

$$V(\boldsymbol{\lambda}, E) = \max_{a \in \{0, 1, \dots, N\}} \left\{ \sum_{k=0}^L u_k^{(a)} \max_{\phi(k) \in \{0, 1\}} [R_{E,k}^{(a,\phi(k))} + V(\mathcal{T}_\lambda(\boldsymbol{\lambda} | a, k), \mathcal{T}_E(E | a, k, \phi(k)))] \right\}. \quad (12)$$

Note that the maximization in (12) is taken over the space with size  $\mathcal{O}(2NL)$  increasing linearly with the number  $L$  of power levels, while that in (10) is taken over the action space  $\mathcal{A}$  whose size  $\mathcal{O}(N2^L)$  increases exponentially with  $L$ .

In Proposition 1, we show that the optimal access decision  $\Phi_a^*$  for sensed channel  $a$  is of threshold type.

*Proposition 1:* Given the belief state  $\lambda$  and the residual energy level  $E$  of the secondary user at the beginning of a slot, there exists a threshold  $k_a^*$  associated with sensing action  $a \in \{1, \dots, N\}$  such that the optimal access decision  $\Phi_a^* = [\phi_a^*(1), \dots, \phi_a^*(L)]$  is given by

$$\phi_a^*(k) = \begin{cases} 1, & \text{if } k \leq k_a^*, \\ 0, & \text{if } k > k_a^*, \end{cases} \quad (13)$$

*Proof:* Assume  $\phi_a^*(k_a^*) = 1$  for some  $1 \leq k_a^* \leq L$ . For any  $1 \leq k \leq k_a^*$ , we have  $\varepsilon_k \leq \varepsilon_{k_a^*}$ . From (5), we have  $\mathcal{T}_E(E | a, k, 1) \geq \mathcal{T}_E(E | a, k_a^*, 1)$  and  $\mathcal{T}_E(E | a, k, 0) = \mathcal{T}_E(E | a, k_a^*, 0)$ . From (8), we have  $\mathcal{T}_\lambda(\boldsymbol{\lambda} | a, k) = \mathcal{T}_\lambda(\boldsymbol{\lambda} | a, k_a^*)$ . Combining the above observations and noting that the total expected reward  $V(\boldsymbol{\lambda}, E)$  increases with  $E$  for any fixed  $\boldsymbol{\lambda}$ , we can show that  $B_a + V(\mathcal{T}_\lambda(\boldsymbol{\lambda} | a, k), \mathcal{T}_E(E | a, k, 1)) \geq V(\mathcal{T}_\lambda(\boldsymbol{\lambda} | a, k), \mathcal{T}_E(E | a, k, 0))$ . Therefore  $\phi_a^*(k) = 1$  for any  $1 \leq k \leq k_a^*$ . The existence of  $k_a^*$  follows from the fact that there are a finite number of observations.  $\square$

Proposition 1 can help us avoid the search for optimal access decisions in some scenarios, resulting in further complexity reduction. Specifically, for each sensing action  $a \neq 0$ , we can calculate the optimal access decisions  $\phi_a^*(k)$  in a decreasing order of sensing outcome  $k$ . Once we have  $\phi_a^*(k^*) = 1$  for a certain value of  $k^*$ , we can determine the optimal access decisions for all remaining sensing outcomes  $k < k^*$  without further computation.

## C. Reduction of Belief State Dimension

Assume that the spectrum occupancy evolves independently across channels. It has been shown in [7] that  $\boldsymbol{\omega} \triangleq [\omega_1, \dots, \omega_N]$ , where  $\omega_n$  denotes the probability (conditioned on all previous decisions and observations) that channel  $n$  is available at the beginning of a slot prior to the state transition, is a sufficient statistic to belief state  $\boldsymbol{\lambda}$ . Note that the dimension of  $\boldsymbol{\omega}$  increases linearly  $\mathcal{O}(N)$  with the number  $N$  of channels while that of  $\boldsymbol{\lambda}$  increases exponentially  $\mathcal{O}(2^N)$ .

Applying the belief state  $\boldsymbol{\omega}$ , we can simplify the value function given in (12). Specifically, let  $\alpha_n = \Pr\{S'_n = 1 | S_n = 0\}$  denote the probability that channel  $n$  transits from 0 (busy) to 1 (idle)

and  $\beta_n = \Pr\{S'_n = 1 | S_n = 1\}$  the probability that channel  $n$  remains idle. Then, (12) reduces to

$$\begin{aligned} \hat{V}(\boldsymbol{\omega}, E) &= \max_{a \in \{0, 1, \dots, N\}} \{(1 - \omega'_a) \\ &\quad \times \hat{V}(\hat{\mathcal{T}}_\lambda(\boldsymbol{\lambda} | a, 0), \mathcal{T}_E(E | a, 0, 0)) \\ &\quad + \omega'_a \sum_{k=1}^L p_a(k) \max_{\phi(k) \in \{0, 1\}} [R_{E,k}^{(a,\phi(k))} \\ &\quad + \hat{V}(\hat{\mathcal{T}}_\lambda(\boldsymbol{\lambda} | a, k), \mathcal{T}_E(E | a, k, \phi(k)))]\}, \end{aligned} \quad (14)$$

where  $\omega'_0 \triangleq 0$ ,  $\omega'_a = \omega_a \beta_a + (1 - \omega_a) \alpha_a$  ( $a \in \{1, \dots, L\}$ ) is the probability that channel  $a$  is available in the current slot given  $\boldsymbol{\omega}$ ,  $\mathcal{T}_E(E | a, k, \phi_a(k))$  is the reduced battery energy given in (5), and the updated belief state  $\hat{\boldsymbol{\omega}} \triangleq [\omega_1, \dots, \omega_N] = \hat{\mathcal{T}}_\lambda(\boldsymbol{\lambda} | a, k)$  is given by

$$\hat{\omega}_n = \begin{cases} 0, & \text{if } a \neq 0, n = a, k = 0, \\ 1, & \text{if } a \neq 0, n = a, k \neq 0, \\ \omega'_n, & \text{otherwise.} \end{cases} \quad (15)$$

## V. SUBOPTIMAL ENERGY-CONSTRAINED OSA

From (10), we notice that the optimal sensing and access decisions in a slot rely on the value functions of all possible information states in the remaining slots, which significantly increases the computational complexity of the optimal policy. In this section, we provide a suboptimal solution to energy-constrained OSA, which reduces the number of value functions used in decision-making. We show that the computational complexity of this suboptimal strategy can be traded off with its performance.

### A. The Greedy- $w$ Approach

Referred to as greedy- $w$  approach, the proposed strategy maximizes the total expected reward in a time window of  $w$  slots. Let  $Y_w^{(a)}(\boldsymbol{\lambda}, E)$  denote the maximum reward that can be accumulated in a window of  $w$  slots given information state  $(\boldsymbol{\lambda}, E)$  and sensing action  $a$ . We can calculate  $Y_w^{(a)}(\boldsymbol{\lambda}, E)$  recursively by

$$\begin{aligned} Y_0^{(a)}(\boldsymbol{\lambda}, E) &= 0 \\ Y_w^{(a)}(\boldsymbol{\lambda}, E) &= \sum_{k=0}^L u_k^{(a)} \max_{\phi(k) \in \{0, 1\}} [R_{E,k}^{(a,\phi(k))} \\ &\quad + \max_{b \in \{0, 1, \dots, N\}} Y_{w-1}^{(b)}(\mathcal{T}_\lambda(\boldsymbol{\lambda} | a, k), \mathcal{T}_E(E | a, k, \phi(k)))], \end{aligned} \quad (16)$$

where  $u_k^{(a)}$ ,  $\mathcal{T}_\lambda(\boldsymbol{\lambda} | a, k)$ , and  $\mathcal{T}_E(E | a, k, \phi(k))$  are given in (11), (8), and (5), respectively. From (16), we can see that for any  $w$ ,  $Y_w^{(a)}(\boldsymbol{\lambda}, E) = 0$  if  $E < e_s + \varepsilon_1$ .

Given belief state  $\boldsymbol{\lambda}$  and residual energy  $E$  of the secondary user at the beginning of a slot, the greedy- $w$  approach chooses channel  $a_w$  that maximizes the reward obtained in the next  $w$  slots to sense, i.e.,

$$a_w = \arg \max_{a \in \{0, 1, \dots, N\}} Y_w^{(a)}(\boldsymbol{\lambda}, E). \quad (17)$$

Given sensing outcome  $k \in \{1, \dots, L\}$ , the access decision  $\phi_{a_w}(k)$  of the greedy- $w$  approach is given by

$$\begin{aligned}\phi_{a_w}(k) &= \arg \max_{\phi \in \{0,1\}} \{R_{E,k}^{(a_w,\phi)} \\ &+ \max_{b \in \{1, \dots, N\}} Y_{w-1}^{(b)}(\mathcal{T}_\lambda(\boldsymbol{\lambda} | a_w, k), \mathcal{T}_E(E | a_w, k, \phi))]\}.\end{aligned}\quad (18)$$

Since its channel selection is determined by the information state  $(\boldsymbol{\lambda}, E)$ , the greedy- $w$  approach ensures transceiver synchronization as shown in Section III-C.

Next, we consider two extreme cases of the greedy- $w$  strategy.

*Case 1:* When  $w = 1$ , the greedy-1 approach focuses solely on maximizing the immediate reward. Specifically, the secondary user employing greedy-1 approach chooses the channel with the maximum expected immediate reward and transmits whenever the channel is sensed to be available:

$$\begin{aligned}a_1 &= \arg \max_{a \in \{1, \dots, N\}} \sum_{k=1}^L u_k^{(a)} R_{E,k}^{(a, \phi_{a_1}(k))}, \\ \phi_{a_1}(k) &= 1_{[k \neq 0]}.\end{aligned}\quad (19)$$

The greedy-1 approach has the lowest computational complexity but worst performance as illustrated in Fig. 1.

*Case 2:* Consider the case when window size  $w$  exceeds the maximum battery lifetime of the secondary user. In this case, the network reaches a terminating state in less than  $w$  slots regardless of the sensing and access strategies. Since no reward is accumulated after the network reaches a terminating state, the greedy- $w$  approach is equivalent to the optimal strategy.

### B. Complexity Vs. Performance

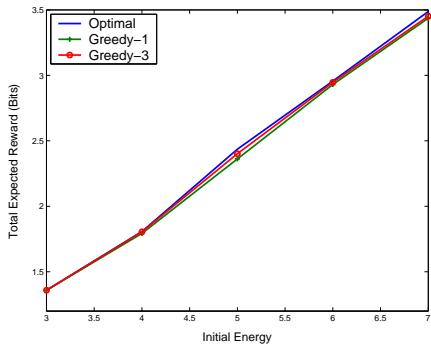


Fig. 1. The number of information bits that can be transmitted by the secondary user during its battery lifetime.  $N = 2$ ,  $[B_1, B_2] = [1, 1]$ ,  $[\alpha_1, \alpha_2] = [0.2, 0.6]$ ,  $[\beta_1, \beta_2] = [0.8, 0.8]$ ,  $e_s = 0.5$ ,  $e_p = 0.1$ ,  $L = 2$ ,  $\mathcal{E}_{\text{tx}} = \{1, 2\}$ ,  $p_n(1) = 0.8$ ,  $p_n(2) = 0.2$  for  $n = 1, 2$ .

We can see from (17) and (18) that the sensing and access decisions made by the greedy- $w$  approach in a slot only depend on the value functions of all possible information states in the next  $w$  slots. Hence, the total number of value functions required to determine the sensing and access decisions during battery lifetime  $T$  is on the order of  $\mathcal{O}((N(L+1))^{w-1}T)$ , which is linear in  $T$ . Clearly, the computational complexity of greedy- $w$  approach increases with  $w$ .

Next, we compare the performance of the greedy- $w$  approach with the optimal performance  $V(\boldsymbol{\lambda}_0, \mathcal{E}_0)$ . In Fig. 1, we plot the

total expected number of information bits that can be delivered by the secondary user during its battery lifetime as a function of the initial energy  $\mathcal{E}_0$ . We consider  $N = 2$  independently evolving channels with different occupancy dynamics. As the window size  $w$  increases, the performance of the greedy- $w$  approach improves. It quickly approaches the optimal performance as  $w$  increases.

The above observations show that the computational complexity of the greedy- $w$  approach increases while its performance loss as compared to the optimal performance decreases as the window size  $w$  increases. Hence, by choosing a suitable  $w$ , the greedy- $w$  approach can achieve a desired tradeoff between complexity and performance.

## VI. NUMERICAL EXAMPLES

Careful inspection of (10) reveals that a sensing and access action  $(a, \phi) \in \mathcal{A}$  affects the total expected reward in three ways: 1) it acquires an immediate reward  $R_{E,k}^{(a, \phi(k))}$  in this slot; 2) it transforms the current belief state  $\boldsymbol{\lambda}$  to  $\mathcal{T}_\lambda(\boldsymbol{\lambda}, a, k)$  which summarizes the information of spectrum occupancy up to this slot; 3) it causes a reduction in battery energy from  $E$  to  $\mathcal{T}_E(E, a, k, \phi(k))$ , leading to a shorter remaining battery lifetime. Hence, to maximize the total expected reward during battery lifetime, the optimal sensing and access policy should achieve a tradeoff among gaining instantaneous reward, gaining information for future use, and conserving energy. In this section, we study the impact of spectrum occupancy dynamics, channel fading statistics, and energy consumption characteristics on the optimal sensing and access actions.

**To sense or not to sense?** The secondary user may choose to sense in order to gain immediate reward and channel occupancy information, but not to sense in order to conserve energy. Hence, the optimal decision on whether to sense should strike a balance between gaining reward/information and conserving energy. In Fig. 2, we study the optimal sensing decision  $1_{[a^* \neq 0]}$  in a particular slot under different spectrum occupancy dynamics and belief states.

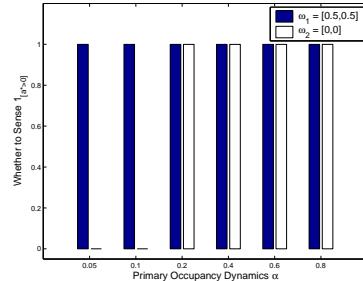


Fig. 2. The optimal decision  $1_{[a^* \neq 0]}$  on whether to sense under different spectrum occupancy dynamics and belief states.  $N = 2$ ,  $[B_1, B_2] = [1, 1]$ ,  $\mathcal{E}_0 = 4$ ,  $e_s = 0.6$ ,  $e_p = 0.1$ ,  $L = 2$ ,  $\mathcal{E}_{\text{tx}} = \{1, 2\}$ ,  $p_n(1) = p_n(2) = 0.5$  for  $n = 1, 2$ .

We consider  $N = 2$  independently evolving channels with identical spectrum occupancy dynamics  $\alpha_1 = \alpha_2 = \alpha$  and  $\beta_1 = \beta_2 = \beta$ . We assume that  $\beta = 1 - \alpha$ . Hence, the stationary distribution of spectrum occupancy state  $\mathbf{S}$  is given by  $\omega_1 = [0.5, 0.5]$ . Consider another belief state  $\omega_2 = [0, 0]$  with

which the secondary user has full information on the spectrum occupancy prior to the state transition in this slot. Conditioned on the belief states at the beginning of this slot, the conditional probability that channel  $n$  is available can be calculated as  $\Pr\{S_n = 1 | \omega_1\} = 0.5$  and  $\Pr\{S_n = 1 | \omega_2\} = \alpha$  for  $n = 1, 2$ . From Fig. 2, we find that the secondary user chooses not to sense only when the conditional probability  $\Pr\{S_n = 1 | \omega\}$  that the channel is available is very small. We also find that the secondary user always chooses to sense if the belief state is given by the stationary distribution  $\omega_1$  of the spectrum occupancy dynamics. The reason behind this is the monotonicity of the value function  $\hat{V}(\omega, E)$  in terms of battery energy  $E$ . Specifically, if the secondary user chooses not to sense, then its belief state at the beginning of next slot will remain  $\omega_1$  but its battery energy will be reduced by  $e_p$  due to energy consumption in the sleeping mode. The maximum total expected reward that can be obtained is thus given by  $\hat{V}(\omega_1, E - e_p)$ . Since  $\hat{V}(\omega, E)$  increases with the battery energy  $E$  for every fixed  $\omega$ , we have  $\hat{V}(\omega_1, E) \geq \hat{V}(\omega_1, E - e_p)$  and hence the secondary user should choose to sense whenever it has a stationary belief state.

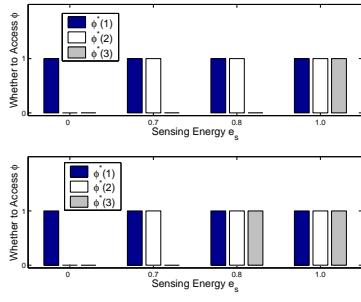


Fig. 3. The optimal access decision under different sensing energy consumptions  $e_s$  and channel fading statistics.  $N = 2$ ,  $[B_1, B_2] = [1, 1]$ ,  $\mathcal{E}_0 = 8$ ,  $e_p = 0.1$ ,  $L = 3$ ,  $\mathcal{E}_{tx} = \{1, 2, 3\}$ . In the upper plot,  $p_n(1) = 0.5$ ,  $p_n(2) = 0.3$ ,  $p_n(3) = 0.2$  for  $n = 1, 2, 3$ . In the lower plot,  $p_n(1) = 0.3$ ,  $p_n(2) = 0.3$ ,  $p_n(3) = 0.4$ .

**To access or not to access?** Without an energy constraint, the secondary user should always access the channel that is sensed to be available. However, under the energy constraint, the access decision should take into account both the energy consumption characteristics and the channel fading statistics. For example, when the sensed channel is available but has poor fading condition, should the secondary user access this channel to gain immediate reward or wait for better channel realizations to conserve energy? In Fig. 3, we study the optimal access decision  $\phi^*$  under different sensing energy consumptions  $e_s$  and channel fading statistics  $\{\phi_n(k)\}_{k=1}^L$ . We find that when sensing energy consumption  $e_s$  is negligible, the secondary user should refrain from transmission under poor channel conditions and wait for the best channel realization. However, when  $e_s$  is large, it should always grab the instantaneous opportunity regardless of the fading condition because the sensing energy consumed in waiting for the best channel realization may exceed the extra energy consumed in combating the poor channel fading.

The access decision should also take into account the channel fading statistics. Comparing the optimal access decisions in the upper and the lower plots of Fig. 3 when sensing energy is  $e_s = 0.8$ . We find that if the probability that the channel expe-

riences deep fading is small (see the upper plot), the secondary user should avoid transmitting under poor channel realizations because the waiting time for a better channel realization is short and hence the energy wasted in waiting can still be lower than the extra energy needed to combat the poor channel condition. On the other hand, if the channel tends to have poor fading conditions (see the lower plot), the secondary user should focus on gaining immediate reward because of the long waiting time for better channel realizations.

## VII. CONCLUSION

In this paper<sup>2</sup>, we obtained the optimal sensing and access policy for energy-constrained OSA by formulating the resulting problem as an unconstrained POMDP. We proposed a suboptimal solution, called greedy- $w$ , whose computational complexity can be systematically traded off with its performance. Numerical results demonstrated that the optimal sensing and access decisions should take into account not only the spectrum occupancy dynamics but also the channel fading statistics and the energy consumption characteristics of the secondary user.

Throughout this paper, we have assumed perfect spectrum sensing, *i.e.*, the sensing outcome reflects the true channel state. Our future work on energy-constrained OSA will address the design of spectrum sensing and access policy in the presence of spectrum sensing errors.

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